

Revue Internationale de

ISSN 0980-1472

systemique

Vol. 12, N° **3**, 1998

afcet

DUNOD

AFSCET

Revue Internationale de
systemique

Revue
Internationale
de Sytémique

volume 12, numéro 3, pages 285 - 312, 1998

A concept of complexity
for the social sciences

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Numérisation Afscet, août 2017.



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A CONCEPT OF COMPLEXITY FOR THE SOCIAL SCIENCES ^(*)

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Résumé

Tandis que la plupart des approches de la "complexité" tente de traiter ce concept comme une propriété inhérente au système observé, cet article considère la complexité comme étant propre à la relation entre un système et son observateur. Il y est affirmé que le concept de complexité doit être utilisé pour mesurer la fiabilité qu'un individu accorde au modèle de classification qu'il adopte pour extraire 'les événements' d'expériences empiriques. La complexité ne peut être définie sans modélisation antérieure des processus cognitifs d'un individu.

En supposant la connaissance des catégories mentales grâce auxquelles un individu perçoit la réalité, une mesure quantitative de la complexité est définie. Et il est démontré que sa valeur numérique peut être utilisée pour évaluer les modes de comportements alternatifs. En particulier, la complexité est capable de rendre compte des caractéristiques de la prise de décision dans des situations où la réalité empirique génère continuellement de nouveaux incidents comme c'est souvent le cas en sciences sociales.

En conclusion, une comparaison est faite à partir des théories de la complexité répandues en physique, science de l'information et biologie. Bien que la plupart de ces théories considère la complexité comme une propriété inhérente au système, elles peuvent être tenue comme une approximation de la complexité présentée ici.

^(*) I wish to thank Kai Brandt, Marcello Cini, Massimo Egidi, Yuri Ermoliev, Walter Fontana, Hermann Haken, Michael Landesmann, Axel Leijonhufvud, Joanne Linnerooth-Bayer, Luigi Marengo and Warren Sanderson for helpful comments and remarks.

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Abstract

While most approaches to the idea of "complexity" attempt to handle this concept as an inherent property of the system under observation, this article considers complexity to be a property of the relationship between a system and its observer. It is argued that the concept of complexity must be used to measure the reliability an individual attaches to the classification model that he or she adopted in order to extract 'events' from empirical experiences. Complexity cannot be defined without previously modelling the individual's cognitive processes.

By assuming a knowledge of the mental categories by which an individual perceives reality, a quantitative measure of complexity is defined, and it is shown that its numerical value can be used to evaluate alternative patterns of behaviour. In particular, complexity is able to account for features of decision-making in situations where empirical reality continuously generates facts of a novel kind, as is usual in the social sciences.

Finally, a comparison is drawn with theories of complexity used in physics, computer science and biology. Although most of these theories handle complexity as an inherent property of the system under observation, it is argued that they can be considered as approximations of the concept of complexity presented here.

1. SELF-REFERENTIALITY

The Cretan philosopher Epimenides (VI century B.C.) left, among his writings, a fragment where he claims that "All Cretans are liars". This seemingly simple statement originated what is known today as 'the Epimenides paradox': If Epimenides' claim is true, that is, if all Cretans lie, then Epimenides too, who is a Cretan, is lying. Thus, Cretans tell the truth. But if Cretans tell the truth, so does Epimenides. Hence, all Cretans lie.

That of Epimenides is only the first of a long series of self-referential paradoxes invented along the centuries. Alfred Whitehead and Bertrand Russell pointed to their common structure, which formally consists of a set containing some elements that are defined in reference to the set itself. Whitehead and Russell (1910, p. 37) noted that, if one claims that a collection of propositions contains a proposition stating that 'all propositions are either true or false', such a statement could not be legitimate unless "all propositions" refers to some already definite collection; which is not possible, since a statement about "all propositions" is itself a new proposition, which can also be false.

This article draws on the analogy between self-referentiality in formal systems and self-referentiality in human societies, and claims that self-referentiality is the core of the concept of complexity: Only when the difficulty to

describe a system is due to the presence of a self-referential paradox are we allowed to speak of 'complexity', rather than of 'complication'. Clearly, this statement is not compatible with viewing complexity as an intrinsic property of a system, like mass or volume. Rather it implies that complexity arises from the interaction between a system and its observer, when in such an interaction it is in principle impossible for the observer to contemplate all the possible reactions of the system to the actions he could undertake upon it.

As F. J. Varela pointed out, already at the level of molecular organisation self-referentiality is what distinguishes living organisms from inanimate objects (Varela, 1979). In aggregates of highly sophisticated living organisms as human societies, self-reference arises from the very fact that the members of a society have imaginative capabilities about its possible arrangements. The possibility of the emergence of new arrangements of society can generate a number of self-referential loops and, consequently, logical indeterminacy. In order to keep the matter tractable, we will limit our analysis to the complexity which can arise between a generic 'social system' and its 'observer', where one single self-referential loop can occur.

Instead of defining the "complexity" the system should possess, we will focus on the adjective 'complex' the observer of a system may attach to it: Let us say that a social system is viewed as "complex" by its observer, when the behaviour of the social system depends on what it "imagines" the observer is imagining. A process of the kind "I think that you think that I think that ..." is clearly a self-referential loop; it also suggests that, besides the complexity of a system seen by its observer, we might speak of the complexity of the observer "seen" by the system as well.

R. E. Lucas' famous statement about the impossibility of using econometric models to evaluate the effects of alternative economic policies (Lucas, 1976) can be seen as derived from the recognition of the complex nature of the interaction between a Government and the economy it is supposed to control. In fact, what Lucas claims is that the reaction of the economic system to the Government's actions depends on what economic agents imagine about the possible actions of the Government, which in turn depends on what the Government imagines about the possible reactions of other economic agents, and so on endlessly like in all self-referential loops.

The logical limits engendered by self-referential loops become clear when they are analysed within the framework of formal logic, where self-referential loops are exploited in Gödel's theorem, which states that in any formal system there are true propositions that cannot be proven. However, considering self-referentiality within the framework of logic is important not only because we

can stress the logical limits of decision-making, but also because it enables us to understand how a self-referential paradox can be overcome, and at what cost.

J. P. Dupuy observes that, in order to overcome the paradoxes caused in decision-making by self-referentiality, the crucial point to keep in mind is that any undecidability problem refers to a particular formal system: in fact, for any proposition that cannot be proven within some formal system, some other formal system exists where that very same proposition can be proven (Dupuy, 1982).

Formal systems differ in the propositions they take as axioms, just like scientific theories differ about what should be regarded as invariant properties, and more generally about which are the relevant aspects of reality. Since a particular undecidability problem disappears if one frames reality in another way, the way out of self-referential paradoxes consists of re-defining which propositions must be regarded as "axioms", as well as which rules these axioms must obey.

Lucas takes exactly this way out of the self-referential paradox posed by economic policy when he wishes that the Government and the other economic agents make joint decisions in accordance with the principles of neoclassical economic theory, so that their effects are foreseeable, in the sense that there exists an agreement between all the actors regarding their behaviours (Lucas, 1976). In fact, this corresponds to choosing neoclassical economic "laws" as "axioms", and to fixing the way they must be used in social interactions. However, Lucas' choice is not unique, since in practice nothing prevents economic agents from establishing agreements which do not necessarily obey neoclassical prescriptions.

In any case, self-referential loops force decision-makers to acknowledge their limits and to reshape the decision process. In the framework which will be used in the subsequent sections, re-shaping the decision process means that the observer of a system re-defines the mental categories by which he perceives it.

This is a problem which will not be tackled by this article, however. It will focus instead on the reliability an individual attaches to the model of the world he relies upon, a reliability which can be undermined by the indeterminacy caused by a self-referential loop. Essentially, this subjective sense of the reliability of the way in which an observer represents a system in his own mind is what will be meant by "complexity".

Section 2 contains some basic assumptions about human cognitive processes that underlie the measure of complexity presented in section 3. Section 4 analyses the implications of this measure of complexity for decision theory, while sections 5 and 6 investigate the links with other concepts of complexity, used in disciplines other than social ones.

2. ASSUMPTIONS ABOUT THE COGNITIVE PROCESSES

The view of complexity as a property of the relationship between a system and its observer is originally due to R. Rosen (Rosen, 1985), who argues that an observer sees a system as 'complex' when he has more than one single description of it, and these descriptions cannot be reduced to only one. The point is not to have some alternative models of the same system, each with a certain probability to turn out to be the right one; rather, a system is seen as "complex" by its observer when, due to the presence of a self-referential loop, the observer can never compile a finite list of the behaviours the system will exhibit.

In this situation it is not possible to neglect the distinction between the system's behaviour, which can exhibit unpredictable and novel features, and the relatively stable mental categories by which the observer perceives this very behaviour. When dealing with complex systems, "events" cannot be considered as objects existing by themselves in empirical reality; rather, they must be recognised as the product of the classifying activity of the human mind. Individuals must first of all decide which phenomena are repetitions of a smaller number of abstractly defined 'events': only thereafter can they apply inferential methods to discover statistical or deterministic laws, and eventually revise the adopted definition of events depending on the extent to which these laws fit reality. For example, F. H. Knight pointed out that it is up to the entrepreneur to form categories of investment types, before calculating anything like a probability distribution of successes and failures (Knight, 1921).

In our framework 'events' are mental categories constructed by the mind of individuals in order to classify empirical facts that are not only very large in number, but also unknown and unpredictable because in the social system a number of novel qualities continuously emerge. These categories do change in order to be able to discriminate the relevant features of qualitatively new empirical facts, yet at a slower time scale than empirical facts themselves: otherwise, they could not be used as classification devices. We will claim that the observer of a system says it is "complex" when empirical facts are such that they do not fit well into the categories by which he tries to understand the system.

Thus, complexity can be quantified upon description of the mental categories employed by an individual, of the relationships occurring between them, and of the extent to which they are appropriate in providing an orientation to the individual's decision-making. In order to provide a clear framework for this task, let us first of all define a few key-concepts:

action: The behaviour of an individual towards the rest of the social system. An individual's actions can undergo unpredictable qualitative changes; in this respect, our "actions" are basically different from Savage's "acts" (Savage, 1954).

result: The reaction of the social system to an individual's action on it. Like actions, results can undergo unpredictable qualitative changes; thus, they are basically different from Savage's "consequences" (Savage, 1954).

empirical fact: An 'empirical fact' is a pair constituted by an action and a result. Being composed of actions and results, empirical facts can also undergo unpredictable qualitative changes (e.g. emergence of new ideas, new technologies, etc.).

mental category: Mental categories have the purpose of enabling the individual to distinguish actions and results according to the features which are relevant to the problems he has to face; they can be seen as "containers" to classify the facts provided by empirical experience. However, mental categories should not be conceived as containers operating according to some similarity criteria fixed once and for all; rather, the categories the mind forms depend on the empirical facts it receives as input, and the shape of these mental categories may not even be precisely defined, since the boundaries between them can be fuzzy. Furthermore, although most mental categories are organised around a prototype, not all the members of a category need to be similar to one another: sometimes, they have some similarity with only some of the other members of the category, but not with all of them (Lakoff, 1987).

event: An 'event' is a pair constituted by an action category and a result category: note that events are the product of the classifying activity of human mind, they are not givens in the empirical reality. We say that the same event occurred two times, if and only if two empirical facts occurred, which differed only in features which were felt to be irrelevant for the decision problems at hand, so that they could be classified in the same mental category.

mental model: P. N. Johnson-Laird showed that human behaviour can be more easily explained by assuming that the mind constructs mental models of reality, rather than by assuming the existence of a "mental logic" (Johnson-Laird, 1983). Such mental models must not be thought of as being able to pro-

duce the correct behaviour in any possible situation, but only in most of the situations the individual usually encounters. With reference to the basic ideas of connectionism (Hebb, 1949; von Hayek, 1952), we can think mental categories as implemented by paths in which information flows in closed loops, and mental models as connections between these categories (Hayek calls "map" the set of the mental categories, and "model" the set of the connections between them).

At this point, let us make the following assumptions about the social system and about the cognitive processes of its members:

A. 1

We will consider the point of view of a single individual towards the rest of the social system. This is the simplest application of the system-observer scheme; eventual extensions to more detailed analyses would require: 1) Consideration of observers, like firms or governments, composed by many individuals; 2) Consideration of the single members of the social system, and of their points of view as observers of what they define as "social system" in turn.

Our individual-observer interacts with the social system by undertaking 'actions' and obtaining 'results' which can undergo unpredictable qualitative changes with time; therefore, no "set of the states of the world" can be specified. On the other hand, description of the individual's mental categories allows specifying the "set of the states of the mind" by which the world is understood.

A. 2

As time goes by, the individual who observes the social system may change the categories he uses to understand reality, creating sub-categories and re-defining the criteria by which actions and results are assigned to existing categories. However, it seems reasonable to assume that the categories by which an individual understands the world change on a slower time scale than the world itself: otherwise it would be hard to imagine how the individual could detect changes of the external reality. For simplifying purposes, let us make this assumption in its extreme form, assuming that the mental categories by which the individual perceive reality do not change at all.

Let $A = \{A_1, A_2, \dots, A_I\}$ be the finite set of mental categories available to the individual-observer to classify the actions he undertakes; let us denote them by an index $i = 1, 2, \dots, I$. Let $R = \{R_1, R_2, \dots, R_J\}$ be the finite set of mental categories

available to the individual-observer to classify the results he obtains; let us denote them by an index $j = 1, 2, \dots, J$. The other individuals or organisations of individuals which constitute the social system may have different categories; however, when information is transferred from the social system to the individual who is observing it, this information is classified according to the individual's categories.

A. 3

The individual is endowed with a memory of finite length L where he stores the data relative to the actions he undertook and to the results he obtained during the last L interactions with the social system. The finiteness of the memory dimension, as well as the finiteness of the number of categories of actions and of results, is an assumption of "bounded rationality" (Simon, 1964; 1972).

The data contained in the memory can be used to measure the probabilities of obtaining a result belonging to category j , provided an action belonging to category i has been undertaken: $p\{A_i \rightarrow R_j\}$. Let us also assume that some utility function is defined on sets A and R . Then, as far as the individual deems that his mental categories appropriately describe the world, traditional decision theory applies, and some objective function (e.g. expected utility) can be evaluated. Up to this point, the only difference with established decision theory (e.g. Savage, 1954) is that these utilities are defined on mental categories, instead of on objects that belong to empirical reality.

However, at each interaction between the individual and the social system he observes, information relative to the action that has been undertaken and to the result that has been obtained enters his memory; at the same time, information that refers to the oldest pair action-result exits it. In this way, the contents of the categories of actions and results change with time, even if the categories themselves do not change.

A. 4

Mental categories are shaped by empirical experience along with the mental model that connects them in order to provide the individual with an orientation device for decision-making. This orientation device consists of specifying which are the categories of results expected from actions belonging to a certain category. In more formal terms, we can say that mental categories are such that some connections between them is expected to occur much more often than the others, and that these connections are what we call 'model of the

world': $\forall A_i, \exists R_j \in R : p^e\{A_i \rightarrow R_j : R_j \in R_i\} \gg p^e\{A_i \rightarrow R_j : R_j \notin R_i\}$, where p^e are probabilities the individual is confident will hold in the future, but that do not necessarily coincide with the probabilities measured in the past.

A. 5

For simplicity, let us assume that the number of categories of actions equals the number of categories of results, and that the model of the world consists of a one-to-one correspondences between them. Fig. (1) shows such a model of the world.

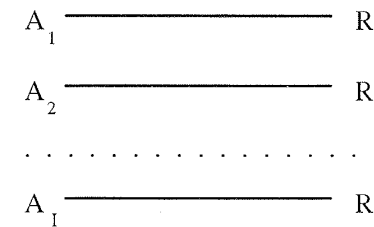


Figure 1.

This model of the world says to the individual that if he undertakes an action belonging to category A_2 , a result belonging to category R_2 is the "normal" outcome (e.g. the expected return of an investment belonging to some category). Let us call this basic model of the world the 'fundamental description' of the system.

A. 6

When correspondences other than those of the fundamental description occur (e.g. A_2 causes R_1), the individual may think that this is just a case which seldom occurs, but which was already considered in the distribution of probabilities $p\{A_i \rightarrow R_j\}$. This would indeed be the only possibility if elementary events were objectively defined in a context where the identification of possible empirical facts was self-evident, as traditional decision theory does.

But in the context we are considering, there is also the possibility that our individual thinks that the mental categories and the model of the world he is using are no longer appropriate to discriminate the relevant features that are emerging in the empirical reality. That is, the individual may think that actions and results underwent such deep qualitative changes, that the categories used to classify them are no longer able to lay stress on the relevant features and to

neglect the irrelevant ones. In this situation, the occurrence of correspondences between categories of actions and of results other than those of the fundamental description, can be interpreted as a consequence of the generation of qualitatively new empirical facts (e.g. in the case of investment decision-making, new goods and new technologies may cause the usual return prospects to not hold). Consequently, a measure of the tightness of the correspondences between categories of actions and categories of results can be taken as a measure of complexity.

A. 7

Individuals calculate probabilities $p\{A_i \rightarrow R_j\}$ using all the data at disposal in their memories, because in this part of the evaluation of empirical information they lay stress on the similarities among empirical facts. But as far as they cast doubts on the appropriateness of the classification criteria that underly these probability distribution, they use the most recent data only, since only these data contain the novel features that are emerging in the empirical reality.

Let us assume that, if M is the number of the most recent memory positions the individual uses to detect eventual novel features of reality, it is $M \ll L$. Looking at the most recent empirical facts, the individual observes whether any correspondences between action categories and result categories occurred, which are not those specified by the fundamental description. If this happened, he measures a complexity greater than zero.

3. COMPUTATION OF COMPLEXITY

Let us now expose the details of the computation of complexity from the most recent M pairs action-result the individual stored in his memory. It might be worth noting that, although the computation of complexity will take the form of an algorithm, Church's thesis is not necessarily implied: as a number of researchers already pointed out (Smolensky, 1986; Harnad, 1990; Mitchell and Hofstadter, 1990) algorithmic computation on abstract symbols defined by the human mind in order to perform high level tasks is perfectly compatible with categorisation, generalisation and induction at a more basic level.

Let us assume that the fundamental description is always at hand in the mind of the individual, no matter whether the pairs (A,R) constituting it are present in his memory, or not. If, in the mind of the individual, some connections between action categories and result categories are recorded, which are not those of the fundamental description, then the correspondences between

action categories and result categories which the individual knows might be for example those depicted in fig.(2):

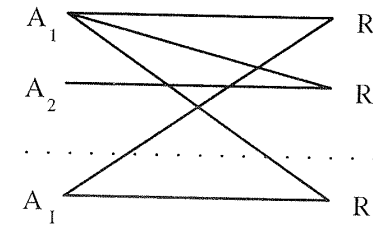


Figure 2.

Let us recall Rosen's definition of complexity reported at the beginning of the previous section: an observer sees a system as 'complex' when he has more than one single description of it. Let us define as 'description of reality' any set of correspondences between action categories and result categories, so that the "fundamental description" we chose as "model of the world" is only one of the many possible descriptions of reality (for simplicity, we assumed that the model of the world coincides with the simplest possible description). Then, complexity is greater than zero when, by selecting some of the correspondences between mental categories that are present in the first M locations of the individual's memory, more than one single description can be constructed. Thus, complexity can be measured by how tightly the A-R relations contained in the first M memory locations are intertwined.

Note incidentally that what matters for complexity computation is whether a pair (A,R) is present at least one time among the last M data of the individual's memory, while it does not matter whether a pair is present one, two, three times, or more. This is a very important point, because it shows that the crucial issue is whether the individual has been surprised by the emergence of some novel feature of reality, while it does not matter at all how many times this novel feature occurred.

In order to measure the tightness of weaves of the kind shown in fig. (2) we will resort to a work of R. Atkin (1975, 1981), who used algebraic topology to represent hierarchical relations between the individuals of a society. Since algebraic topology is also a fundament of Category Theory (Rosen, 1991), it makes sense to apply Atkin's studies to the context of the hierarchies of action categories and of result categories in an individual's mind. The hierarchies investigated herein actually border triviality, having just one single level of action categories and one single level of result categories.

To see the world as complex, that is to consider other descriptions apart from the fundamental one as equally possible, means that at least one action category A_i has correspondences with more than one result category. Let us denote by A and R the sets of action categories and respectively of result categories, and let us denote by R_i the subset of R constituted by the result categories that are in correspondence with A_i , and by A_j the subset of A constituted by the action categories that are in correspondence with R_j . In more formal terms we can say that the individual introduces a relation λ between A and R such that $(A_i, R_j) \in \lambda$ when A_i is in correspondence with a subset of R which contains R_j .

'Simplicial complex' $K_A(R, \lambda)$ represents geometrically relation λ between sets A and R . It is made of so many simplices as elements in A ; vertices of simplex A_i are the elements of R which belong to subset R_i (see appendix A). If the only connections between categories of actions and categories of results are those of the fundamental description, simplices are not connected to one another. On the contrary, if there are also other connections, at least two of the corresponding simplices have at least one vertex in common.

Furthermore, let us represent relation λ also by an incidence matrix Λ of dimensions $I \times J$, whose generic element λ_{ij} takes the values:

$$\lambda_{ij} = \begin{cases} 1 & \text{if } A_i \in A_j \text{ and } R_j \in R_i \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

Let us now consider the dual relation λ^* , defined inverting the roles of sets A and R : now $(R_j, A_i) \in \lambda^*$ when to R_j corresponds a subset of A containing A_i . Dual relation λ^* can be represented by the dual simplicial complex $K_R(A, \lambda^*)$, which has incidence matrix Λ^T . The reason for introducing the dual simplicial complex is that element (i, i') of matrix $\Lambda \Lambda^T$ equals the number of vertices that simplices A_i and $A_{i'}$ have in common. Then, element (i, i') of matrix $\Lambda \Lambda^T$ minus one is the dimension of the eventual common face between simplices A_i and $A_{i'}$. If such a number is negative, then simplices A_i and $A_{i'}$ have no common point.

Let us define the following $I \times I$ matrix:

$$L := \Lambda \Lambda^T - \mathbf{1} \mathbf{1}^T \quad (2)$$

where $\mathbf{1}$ denotes a $I \times 1$ vector of ones. The dimension of the eventual common face between simplices A_i and $A_{i'}$ is then equal to element $L_{ii'}$ of matrix L .

Two simplices having no point in common may nonetheless have common points with other simplices, which in turn do have common points. We say that simplices A_i and $A_{i'}$ are 'q-connected' in $K_A(R, \lambda)$ if there exists a chain of simplices $\{A_{h_1}, A_{h_2}, \dots, A_{h_r}\}$ such that $q = \min\{l_{ih_1}, l_{h_1h_2}, \dots, l_{h_r i'}\} \geq 0$.

Let Q be the dimension of $K_A(R, \lambda)$ the simplex of which has the largest dimension. By inspection of matrix L we can partition the set of simplices that compose $K_A(R, \lambda)$ according to connection level q for $0 \leq \forall q \leq Q$.

Let us introduce a 'structure vector' \mathbf{q} , of dimensions $(Q + 1) \times 1$, and let us denote its q -th component by \mathbf{q}_q . In general, for any connection level q there is some number of disjoint classes of simplices, such that the simplices belonging to a class are connected at that level: the q -th component of structure vector \mathbf{q} is the number of disjoint classes of simplices that are connected at level q .

Simplices connected at level q are obviously connected at level $q - 1$, too. However, in order to avoid repetitions, we do not consider a class of simplices connected at level q to be also a class of simplices connected at levels $q - 1$, $q - 2$, etc. For example, let simplices A_1 and A_2 be connected at level $q = 2$, and let simplex A_3 be connected at level $q = 1$, with A_2 . Then, $\{A_1, A_2\}$ is a class of simplices connected at $q = 2$ and $\{A_1, A_2, A_3\}$ is a class of simplices connected at $q = 1$; however, $\{A_1, A_2\}$ is not a class of simplices connected at level $q = 0$.

The measure of complexity of a simplicial complex is a measure of the extent to which the simplicial complex is connected. Thus, let us consider only the case where the simplices of a simplicial complex are at least connected at level $q = 0$, i.e. where each of them has at least one common point with another simplex. Otherwise, i.e. if $K_A(R, \lambda)$ is made of parts having no point in common, let us agree to take as complexity of $K_A(R, \lambda)$ the largest among the complexities of its parts.

An evaluation of the complexity of Atkin's simplicial complexes can be found in J. Casti (Casti, 1989, p. 410). Here I propose a slight modification of this measure since Casti's formula, for low values of complexity, can attach the same value to very different simplicial complexes:

$$c(K) = \begin{cases} 0 & \text{if } \Lambda \equiv \mathbf{I} \\ \sum_{q=0}^Q \frac{(q+1)}{\mathbf{q}_q} \Big|_{\forall (q, \mathbf{q}_q \neq 0)} & \text{otherwise} \end{cases} \quad (3)$$

This measure of complexity is zero when the simplicial complex reduces to single simplices, each of them being just a point. On the other hand, the largest value complexity can attain depends on the number of categories of actions and of results, which is also the largest possible number of simplices and of their vertices, respectively.

The interpretation of $(q + 1)$ terms is straightforward: the tighter connected the simplices are, the more "complex" the situation is felt by the decision-maker. But decision problems may be very complex in some parts and still very simple in others, in which case only a few simplices are tightly connected, the others being connected pretty much like in the fundamental description. Intuitively, it does not only matter how tightly connected the faces of the simplicial complex are on average, but also whether the simplicial complex looks much like a ball or it has bumps, instead. Terms q_q take account of this second effect on complexity.

Each member of summation (3) represents the contribution to complexity provided by the class of simplices connected at level q , for $q = 0, 1, \dots, Q$. Let us stipulate that, within each class of simplices, the contributions of single action categories are proportional to the dimensions of the corresponding simplices. If at connection level q there is only one class of simplices, this rule gives immediately the contribution to complexity of single action categories. If there are two or more classes of simplices, formula (3) works as if at any q only one of these classes contributes to complexity: in this case, let us stipulate that the corresponding term $(1 + q)/q_q$ be further divided by the number of classes q_q to obtain the contribution of the single classes of simplices, and the resulting complexity be attributed to the single action categories according to the dimensions of their simplices. In this way we obtain the contribution to complexity by category A_i at connection level q , which we denote by $c_q(A_i)$. Contribution to complexity by category A_i is then

$$c(A_i) := \sum_{q=0}^Q c_q(A_i) \quad (4)$$

Appendix A contains a numerical example of the calculation of the complexity of a simplicial complex.

4. INFLUENCE OF COMPLEXITY EVALUATION ON DECISION-MAKING

The purpose of this section is to connect the theory of complexity exposed above to established decision theory, and to point to some possible fields of application.

Complexity measures the confidence an individual attaches to the way he decided to define events by neglecting some features of empirical facts, while stressing others. Once events are defined, usual decision theory applies, and some objective function must be maximised. Let us assume that the most simple objective function, subjective expected utility, is appropriate to evaluate the decision problem as it is defined by the existing mental categories, and let us examine how complexity influences decision-making.

To this aim, let us derive from the complexity attached to a single action category $c(A_i)$ a 'degree of confidence' in the appropriateness of a single action category to the decision problem at hand.

We want this degree of confidence to increase when complexity decreases, and *vice versa*. Furthermore, we require that it ranges within $[0, 1]$ in order to take account of it by means of a simple multiplication with expected utility. Consequently, let us define the degree of confidence attached to action category A_i as follows:

$$\omega(A_i) := 1 - \frac{c(A_i)}{c(K)} \quad (5)$$

The objective function the individual attempts to maximise thus becomes

$$J(A_i) := [\omega(A_i)]^{k(A_i)} \sum_{j=1}^J p\{A_i \rightarrow R_j\} u(R_j) - u(A_i) \quad (6)$$

where exponents $k(A_i)$ have a twofold meaning:

1) The importance that an individual attaches to the degree of confidence depends on his personal attitudes, as well as on the decision problem he faces. For example, investment decisions are much more risky than purchase decisions at the supermarket; consequently, economists speak of the "animal spirits" of entrepreneurs (Keynes, 1936), not of consumers.

2) Degree of confidence should have opposite effects on individual decisions when it refers to a result that is worse than the one foreseen by the fundamental description, and when it refers to a result that is better than the one foreseen by the fundamental description. In the first case, when the degree of confidence is < 1 the objective function should decrease, while in the second case, when the degree of confidence is < 1 the objective function should increase.

Since the fundamental description is a one-to-one correspondence between categories of actions and of results, let us denote by R_i the result category which the fundamental description associates to A_i . Given the disutility associ-

ated with A_i , if utility function has on R_i a value above (under) the average on R_i , the degree of confidence should be such that the value of objective function is lower (higher) than without taking account of it.

From these considerations it is immediate to derive the following expression for the exponent of the degree of confidence:

$$k(A_i) = \zeta(A_i) \frac{u(R_i) - u(A_i)}{\sum_{R_j \in R_i} [u(R_j) - u(A_i)] / \text{card } R_i} \quad (7)$$

where $\zeta(A_i)$ takes account of the individual's attitude towards the degree of confidence on action category A_i , while the second term takes account of the possibility that $\omega(A_i)$ can be referred to a result with utility above or under the average.

It is important to remark that objective function (6) differs from the ones usually used in decision theory, since its arguments are mental categories of actions and of results instead of "acts" and "consequences" given once and for all (like in Savage, 1954). This means that preferences are supposed to be defined on the mental structures by which individuals perceive objects, rather than on the objects themselves.

As long as the model of the world and the underlying mental categories are not discarded, the effect of the degree of confidence is that of introducing sudden jumps in the individual's behaviour, which occur at the moments where correspondences between categories, which are different from those of the fundamental description, enter or exit the first M memory locations. In these moments the degrees of confidence in the action categories can change abruptly to different degrees, making suddenly some action category preferable to the others.

However, an even more important consequence for decision theory is the effect of large values of the overall complexity (3), which refers to the whole representation of reality of an individual. When complexity is high, the mental model and the underlying mental categories do not provide anymore an orientation in a world whose qualitative features continuously change. The individual must re-formulate his mental categories, as well as the model of the world defined upon them; this can lead to the decision to postpone decision-making until the problem will be framed in a more proper way. However, this article does not deal with the modellisation of how mental categories and mental models of the world evolve over time, but only with the recognition of the need to re-formulate them.

A comparison can be drawn with classifier systems (Holland, 1975; 1986), provided we accept a reductive view of mental categories as collections of objects that share some common properties. Then, classifiers can be taken as rudimentary mental categories, the connections between classifiers induced by their "strengths" as the connections between categories that constitute the model of the world, while genetic algorithm is the process whereby categories can be re-formulated. As long as this metaphor holds, we can say that complexity evaluation has the purpose to decide when the genetic algorithm must be activated. However, it is important to stress that, unlike classifier systems, the model presented in this article neither needed to specify the set of the input characters which carry information from empirical reality, nor the length of the strings of these characters. This is an important issue, since if the set of possible input characters and the length of their strings is fixed once and for all, the set of the possible "novelties" which can be discovered is fixed once and for all, too.

Another comparison can be drawn with R. Heiner's remark that an individual may prefer to exclude some action "a" from his repertoire, if he is not always able to discriminate the information which should trigger "a" from the rest, and if undertaking "a" in the wrong occasions causes substantial losses (Heiner, 1983). Even if only in the most recent work Heiner indirectly refers to mental categories instead of to actions specified once and for all (Heiner, 1986), to exclude "a" from the set of the possible actions can be easily interpreted as a particular case of category reformulation. However, Heiner himself (Heiner, 1986, p. 67) points out that the probability that an individual is able to process correctly the information he receives, which has a crucial importance in his theory, can only be evaluated *ex post* by the experimenter who observes decision-making; it cannot be evaluated by the decision-maker himself while he is taking a decision. On the contrary, the complexity and the degree of confidence defined in this article aim to describe the decision process from the point of view of the decision-maker himself.

Situations where self-referential loops generate novel features occur very often in the social sciences; whenever novel features emerge, it makes sense to attach a degree of confidence to the probability distribution of the categories of the results which can be obtained from the action which a decision-maker undertakes.

The theory developed above was referred to the rather abstract situation of a social system observed by a single individual; in reality, agents that observe and attempt to control social systems are more often organisations of individuals. Many scholars in cognitive science, however (Bateson, 1972; Hutchins,

1995), stress the similarity between the mind of a single individual and the "collective mind" of an organisation of individuals. Thus, let us point to situations where it is useful to consider the complexity and the degree of confidence defined above, with the understanding that the same theory applies to collective agents as well:

1) Self-referentiality in the relationship between a Government and the rest of society has been already discussed in §(1), although the argument was limited to the economic domain. The case is actually much more general, 'power' being according to N. Luhmann the capability to reduce complexity by restricting the set of alternatives available to the subordinates (Luhmann, 1975). If the power of a Government resides in its ability to overcome political deadlocks by casting the decision problem in terms such that a unique solution appears feasible, our model says that political decisions are likely to be postponed until the main actors agree on a simple model of the world, of the kind of the "fundamental description" shown in fig.(1).

2) The evaluation of the environmental impact of human activities is open to very many interpretations, since it depends on a huge number of variables, many of them not directly observable. A self-referential loop arises between environmental scientists and the society they are part of, with the consequence that scientists stick on a conventional consensus about the values of some critical magnitudes as they had been estimated at the beginning of environmental research (van der Sluijs, 1997). On the other hand, practical users often attach little confidence to the environmental predictions scientists produce; for example, insurance companies often refuse to stipulate policies against catastrophic environmental risks on the ground that scientific estimates are not reliable enough (Kunreuther, 1996). This kind of behaviour can be explained by the need to reformulate the mental categories the decision problem is cast into, postponing any decision until this task will be accomplished.

3) A firm's behaviour depends on what competing firms do. Due to a self-referential loop between a firm and the industrial system it is part of, strategic decision-making often cannot be univocally determined. If a firm is uncertain about the categories by which it interprets information about current technologies and customers' needs, the sudden jumps of the degree of confidence defined above produce a high variability in decision-making that reminds of the "animal spirits" J. M. Keynes spoke of (Keynes, 1936). Also in this case, in extreme situations an absolute lack of confidence in the model of the world may lead to the decision to postpone any decision. Appendix B discusses this example in detail.

5. RELATIONSHIP TO COMPLEXITY IN CLASSICAL PHYSICS AND IN COMPUTER SCIENCE

The objects studied by classical physics belong to a class of particularly simple systems; essentially, macroscopic bodies moving according to the laws of Newtonian mechanics and thermodynamic systems. Scientific tradition established a univocal identification of elements which, for specific aims, can be considered as the ultimate constituents of these systems. What these constitutive elements do are the 'elementary events' one is concerned with (e.g. positions and velocities of moving bodies); in this context, consideration of the observer's cognitive processes is usually omitted.

Consequently, the relationship between system and observer is trivial; scientific inquiry can focus upon properties of the system which can be considered to be "objective". Computer science also finds itself in a similar situation, since the definition of the set of symbols a computer will manipulate is equivalent to the definition of some "elementary events" all the others are constructed upon.

Since in this situation the observer considers a set of exhaustive events the system can produce, the intuitive idea of complexity as "capacity of a system to surprise its observer" (or similar statements), can be expressed in probabilistic terms. It turns out that, in this context, the traditional concept of 'entropy' is a good starting point for the meaning one would intuitively attach to the term 'complexity', although these two concepts cannot be taken as equivalent.

In fact; let us recall that the immediate meaning of thermodynamic entropy is that of being a measure of the "disorder" of a system: "disorder", in intuitive terms, is supposed to be more "complex" than "order", at least up to the point where disorder is so large that one gives up the hope to understand its laws. Information entropy, in its turn, measures the "disorder" of the information that arrives at the end of a communication channel; it is thus a measure of "lack of information", which is another meaning one would intuitively attach to "complexity". Furthermore, L. Brillouin showed that thermodynamic entropy and information entropy are closely linked, since it is not possible to decrease one without increasing the other: in order to obtain less "disordered" information about a system, we must increase the "disorder" of the system itself (Brillouin, 1956).

Entropy is also linked to the concept of 'computational complexity' of a sequence of characters, introduced by R. J. Solomonoff (1964), A. N. Kolmogorov (1965) and G. C. Chaitin (1966). The computational complexity of a

sequence of characters Y , given a sequence of characters U , is the minimal length of the program h which computes Y knowing U : computational complexity is maximal when there is no simpler way to describe Y than by listing all its characters, because there are no regular patterns in it; which is equivalent to saying that the sequence is "disordered", or that its entropy is maximal.

On the other hand, even if we limit our concern to the systems studied by classical physics, entropy is not a completely satisfactory measure of the meaning we would like to attach to the term "complexity" since some completely disordered systems can only be described by means of statistical averages, like e.g. the molecules of a gas, and are not intuitively perceived to be "complex". Rather, it seems that maximal complexity should lie somewhere between zero and maximal entropy, in the zone where a system is neither so completely ordered that it can be described by simple deterministic laws, nor so completely disordered that it can be described by simple stochastic laws. In this zone, the system does exhibit some structure, which an observer finds very "complex" to describe.

Some measures of complexity have been proposed that take minimum value when entropy is either minimal or maximal, and take maximal value in between; most widely accepted magnitudes are 'logical depth' proposed by C. H. Bennett (1988) and 'statistical complexity' proposed by J. P. Crutchfield and K. Young (1989) (see also Crutchfield, 1994).

The point I make in this article is that these measures of complexity, although correct for the context they have been thought for, are of no use in the social sciences, for the basic reason that they assume the knowledge of the "elementary events" the system can exhibit. In the social sciences this circumstance is negated, and it is necessary to consider the mental categories by which information is perceived, and the different "events" which are defined when categories are formed.

The model presented in the previous sections does not contrast with the ideas that underly Bennett's or Crutchfield's measures of complexity, however. Rather, it can be used to re-interpret their idea of a complexity that is maximal at intermediate entropy values.

In fact, the crucial point of the whole theory of complexity presented in this article is that the individual who is observing a system needs a simple and reliable model of it. When entropy increases over a certain limit, he will re-define the categories by which he is trying to understand the system, switching e.g. from a deterministic microscopic description to a stochastic macroscopic description. Using the new categories, e.g. the macroscopic magnitudes thermodynamics defines, it is easy to describe the system by a simple and reliable

model; in other words, the system does not appear "complex" anymore, once the mental categories to understand it have been changed. In this way, we have zero complexity at the two extremes of zero entropy and maximal entropy; on the contrary, complexity is maximal when entropy has already increased up to quite a high level, while the mental categories are still the initial ones.

Note that a distinctive feature of the "subjective" concept of complexity presented in this article is that it implies that complexity varies through discontinuous jumps. Minor jumps occur whenever correspondences between categories, which are different from those of the fundamental description, enter or exit the first M locations of the individual's memory. Besides, more dramatic jumps occur when new mental categories are defined (e.g. at the passage from a deterministic microscopic description to a stochastic macroscopic description of a physical system). In any case, whereas "objective" measures of complexity like logical depth or statistical complexity vary with continuity, the "subjective" approach presented in this article accounts for abrupt changes in an individual's attitude towards the system he is observing.

6. RELATIONSHIP TO COMPLEXITY IN BIOLOGY

The first attempt to define complexity in biology was that of H. Atlan (1972), who proposed an extension of information theory (Shannon, 1949; Khinchin, 1957) which rests on the unconventional assumption that, in a transmission system, the receiver does not know all the words that the source can emit. This assumption has non-trivial implications for a transmission system which uses a redundant codification: if random disturbances modify the original words transforming them into some of the words that in a redundant codification are not used, the receiver is no longer able to distinguish between the words generated by the random disturbances, and the words actually emitted by the source.

In this way, Atlan can interpret evolution within the framework of information theory, with DNA's nucleic acids as the characters emitted by the source of some transmission system, the living species as the "words", or sequences of these characters (i.e. sequences of nucleic acids of a given length), genetic mutations as the effect of a noisy channel between source and receiver and, finally, the natural environment as the receiver of such a transmission system. Of course, this is a rough schematisation which does not take any account of the very many environmental constraints that influence the passage from phenotype to genotype; however, in principle it would be possible to take account

of these constraints by assuming that some "words" cannot be produced, without any need to change the conceptual framework.

The interesting remark is that, given a certain word length (length of the amino acid sequences), random mutations can create new "species" only at the expense of the words the redundant codification had left unused. For any word length fixed once and for all, the more new words (new species) are generated, the more difficult evolution becomes.

Atlan captures this property of evolutionary dynamics by means of mean mutual information between source and receiver. If any two distant parts of a system are taken as 'source' and 'receiver' and their behaviour is analysed by means of information theory, mean mutual information measures how related these parts are, in the sense that it measures how similarly they behave. It is thus somehow a measure of the structures that are present in the system, and for this reason many other scholars who work on information theory take mean mutual information as a measure of complexity (see Bennett, 1990 for a thorough discussion of this topic).

In the context of Atlan's theory, mean mutual information first increases with time, because of the generation of useful species that diffuse quickly over the whole population; then it decreases, due to the random generation of useless mutants, which is the most that can happen after the redundancy of DNA codification has been exploited. Maximal mean mutual information corresponds to an optimal balance between replication of existing phenotypes, and experimentation with new mutants.

This is consistent with Stuart Kauffman's studies of the shape of the "fitness landscapes" where evolution takes place (Kauffman, 1993). In fact, Kauffman argues that evolution is most effective when the frequency of mutations and the shape of the fitness landscape are balanced in such a way as to avoid on the one hand that the population spreads over all the possible species, no matter how fit they are, and on the other hand to avoid that the whole population concentrates on some species that are far from being the fittest ones. Such a balanced situation, bordering chaos on one side and order on the other, is denoted by Kauffman as a 'complex' one. In other words a "complex" situation, according to Kauffman, is one where mutations do occur, but they are not too many, a situation which corresponds to the maximum of mean mutual information in Atlan.

The concept of complexity defined in this article can be linked to these theories of complexity, too.

From the point of view of an individual who observes a biological system, mutations are novelties that may cause the model of the world not to function anymore, thereby increasing the complexity by which the world is seen. Complexity, as it has been defined in this article, increases by discrete amounts whenever new traits emerge that make the old mental model useless, and decreases abruptly whenever the mental categories are re-formulated and a new model of the world is constructed.

In Atlan's theory, mean mutual information reproduces this pattern, although without the abrupt upward and downward jumps that characterise the measure of complexity presented in this article. Actually even mean mutual information increases by discrete amounts any time a new word is created, although this aspect has not been emphasised by Atlan himself.

The difference with the subjective view of complexity presented in this article derives from the circumstance that in biology, like in classical physics but unlike in the social sciences, it is possible to identify some ultimate particles (nucleic acids) from whose combination all possible novelties can be generated. This allows to construct a theory of complexity which is as "objective" as the ones used in classical physics and in computer science, and which measures complexity by means of a smooth function that does not take account of the observer's cognitive processes.

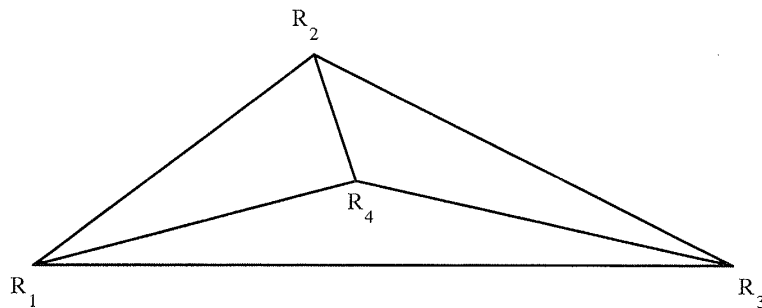
On the other hand, Atlan's hypothesis actually introduces a subjective aspect into the theory by allowing the receiver of a transmission system to evaluate the information carried by "new" words: the surprise caused by new words reminds of the malfunctioning of the model of the world caused by novel features of reality. Like in the social sciences, in Atlan's theory "complexity" is the observer's difficulty to understand the system, but like in classical physics this complexity can be quantified without resorting to the description of what happens in the observer's mind. Under this respect, biology can be ascribed to a status which is somehow intermediate between that of classical physics on one hand, and that of the social sciences on the other.

APPENDIX A

Let relation λ be given by the following incidence matrix:

λ	R_1	R_2	R_3	R_4
A_1	1	0	1	1
A_2	0	1	1	0
A_3	1	0	1	0
A_4	1	1	1	1

Here A_1 is the two-dimensional simplex of vertices R_1, R_3, R_4 ; A_2 is the one-dimensional simplex of vertices R_1 and R_2 , and so on. The simplicial complex can be drawn as follows:



The tetrahedron shown in this picture is simplex A_4 , its faces being simplices A_1, A_2 and A_3 . Matrix L is:

$$L = \Lambda \Lambda^T - \mathbf{1}\mathbf{1}^T = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 0 & 2 & 1 \\ 0 & 1 & 1 & 0 \\ 2 & 1 & 3 & 1 \\ 1 & 0 & 1 & 1 \end{bmatrix}$$

In this case it is $Q = 2$. In order to build structure vector q we note that: at $q = 0$ there is a single class of simplices $\{A_1, A_2, A_4\}$, so that $q_0 = 1$; at $q = 1$ there is a single class of simplices $\{A_1, A_2, A_3, A_4\}$, so that $q_1 = 1$; at $q = 2$ there is a single class of simplices $\{A_1, A_3\}$, so that $q_2 = 1$.

Thus, the structure vector is $q^T = [1 \ 1 \ 1]$. At this point it is trivial to calculate complexity, obtaining $c(K) = 1 + 2 + 3 = 6$.

Contribution to complexity by the single simplices is computed as follows.

at $q = 0$ class of simplices $\{A_1, A_2, A_4\}$ contributes to complexity with $(0 + 1)/1 = 1$. Their relative dimensions are 2:1:3, so at this connection level they contribute to complexity with $c_0(A_1) = 1/3, c_0(A_2) = 1/6, c_0(A_4) = 1/2$;

at $q = 1$ class of simplices $\{A_1, A_2, A_3, A_4\}$ contributes to complexity with $(1 + 1)/1 = 2$. Their relative dimensions are 2:1:1:3, so at this connection level they contribute to complexity with $c_1(A_1) = 4/7, c_1(A_2) = 2/7, c_1(A_3) = 2/7, c_1(A_4) = 6/7$;

at $q = 2$ class of simplices $\{A_1, A_3\}$ contributes to complexity with $(2 + 1)/1 = 3$. Their relative dimensions are 2:1, so at this connection level they contribute to complexity with $c_2(A_1) = 2, c_2(A_3) = 1$.

Thus $c(A_1) = c_0(A_1) + c_1(A_1) + c_2(A_1) = 61/21, c(A_2) = c_0(A_2) + c_1(A_2) = 19/42$ and $c(A_3) = c_1(A_3) + c_2(A_3) = 9/7, c(A_4) = c_0(A_4) + c_1(A_4) = 19/14$ that sum up to $c(K) = 6$.

APPENDIX B

Let us consider a firm's investment decision in a situation where new technologies continuously emerge, and let us model the firm's cognitive apparatus by two categories of actions and two categories of results:

A_- is a category for actions that imply low investments, generally carried out by the firm with its own means; these actions usually do not lead to production and profit expansion, but rather to their stagnation or fall.

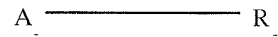
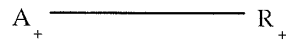
A_+ is a category for actions that imply large investments, generally possible only through bank financing; actions of this kind are undertaken because one expects from them a much better result than from actions of category A_- .

R_- is the category of mediocre results normally expected from actions of category A_- , while obtaining a result of category R_- from an action of category A_+ means the failure of the investment.

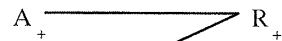
R_+ is the category of good results one expects from actions of category A_+ , while receiving a result of category R_+ from an action of category A_- is a particularly favourable and unexpected event.

Let us assume that past experience be such that it is reasonable to classify actions into "actions implying low investments" and "actions implying high investments", because this leads to a simple model of the world: low invest-

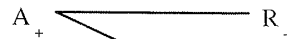
ments caused low gain, high investments caused high gain. If this does not happen anymore, managers may think the causes are some relevant qualitative changes of the production technologies, which are not captured by the extremely rough categories "high investments" and "low investments". Four configurations are possible:



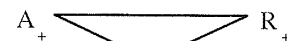
(a)



(c)



(b)



(d)

In case (a), only the connections foreseen by the fundamental description occurred, and the firm casts no doubt upon it. In the other cases, the model of the world is not validated: in case (b) our firm has doubts about the usefulness of the probability distribution of success and failures when it undertakes an action of category A_+ , in case (c) when it undertakes an action of category A_- , while in case (d) doubts are present whatever the firm does.

Degrees of confidence in the four cases take the following values:

$$\text{case (a): } \begin{cases} \omega(A_-) = 1 \\ \omega(A_+) = 1 \end{cases}$$

$$\text{case (b): } \begin{cases} \omega(A_-) = 1 \\ \omega(A_+) = 0 \end{cases}$$

$$\text{case (c): } \begin{cases} \omega(A_-) = 0 \\ \omega(A_+) = 1 \end{cases}$$

$$\text{case (d): } \begin{cases} \omega(A_-) = 0,5 \\ \omega(A_+) = 0,5 \end{cases}$$

Case (a) is trivial: the firm has full confidence in the classification criteria of empirical facts it is using, only the probability distribution of successes and failures influences its decision, traditional decision theory applies.

In cases (b) and (c) the decision taken by the firm is strongly influenced by the degree of confidence.

Case (d) is apparently like (a), because in both cases all what matters is the probability distribution of successes and failures. Yet the difference is that in case (d) a process of category re-formulation is likely to set in, possibly together with the decision to postpone any decision.

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**UN PROJET DE MODÉLISATION DES SYSTÈMES
DE COMMUNICATION : UNE APPROCHE DE LA COMPLEXITÉ
ORGANISATIONNELLE**

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Résumé

Les Systèmes de Communication dans lesquels le sens porté par les acteurs aux différents faits observés est un élément fondamental à prendre en compte ont une complexité organisationnelle très particulière. Nous la qualifions de complexité profonde. Nous comparons l'approche classique de modélisation des Systèmes de Communication avec une modélisation systémique, prenant en compte cette complexité. Nous proposons, dans cette approche, un modèle fondé sur la réification des intentions et motivations des acteurs par un espace de formes dynamiques : des agents adaptatifs coopératifs. Ces perceptions sont alors des connaissances exploitables du système. Nous représentons le sens du phénomène perçu comme des modifications morphologiques dans cet espace de formes.

Abstract

For some Communication Systems, the meaning of observed facts and situations appreciated by the actors is a fundamental character we have to take into account. In such a case, the organizational complexity of the knowledge in the system is very particular, that we call the deep complexity. We compare the classical approach for the modeling of Communication Systems with a systemic one, taking into account this kind of new complexity. We propose a model founded on the reification of actors' intentionality and motivation in a space of dynamic forms : a space of dynamic co-operative agents. These perceptions are used as particular knowledge in the system. We represent the meaning of the perceived phenomena as the morphological transformations of this space of forms.

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